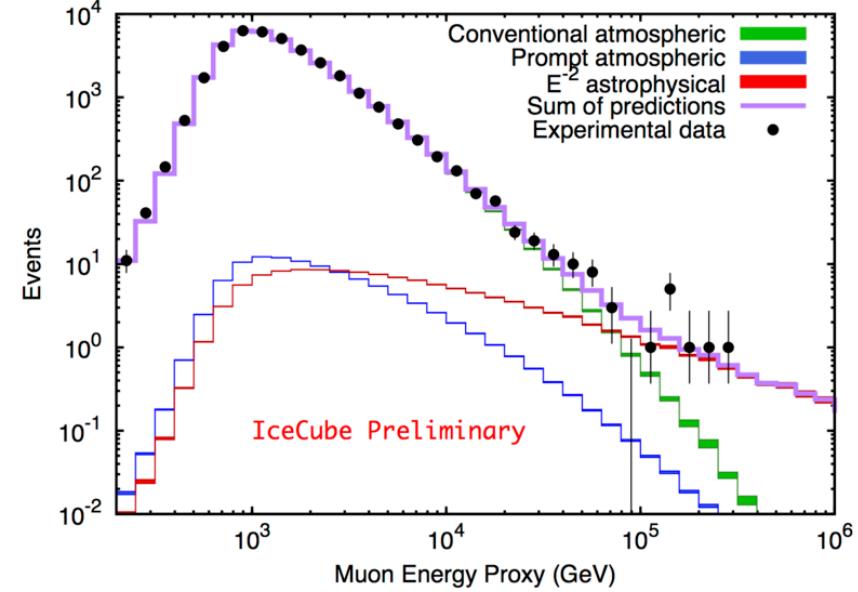
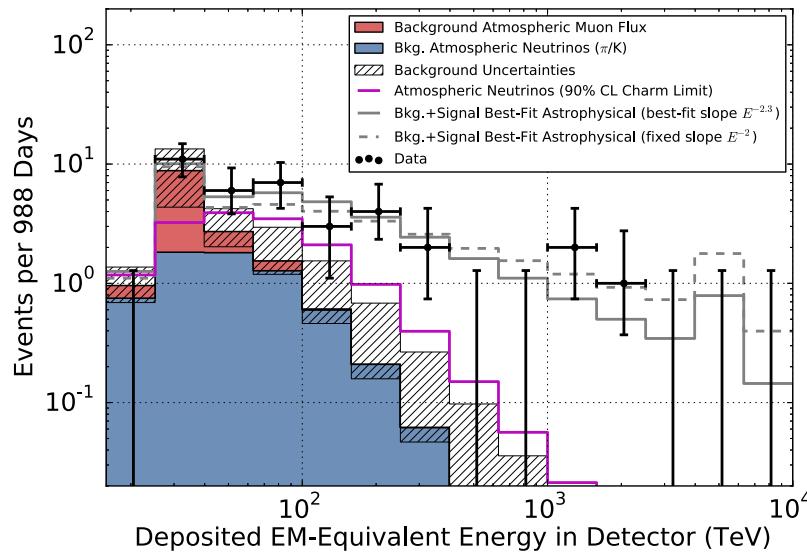


# Atmospheric neutrinos

As background for  
astrophysical neutrinos

# Motivation: IceCube discovery is the high-energy tip of an iceberg: What's below the surface?



IceCube discovery plot. HESE analysis cuts out low energy.  
Index of astro flux  $\sim 2.3$  ?

PRL 113, 101101 (2014)

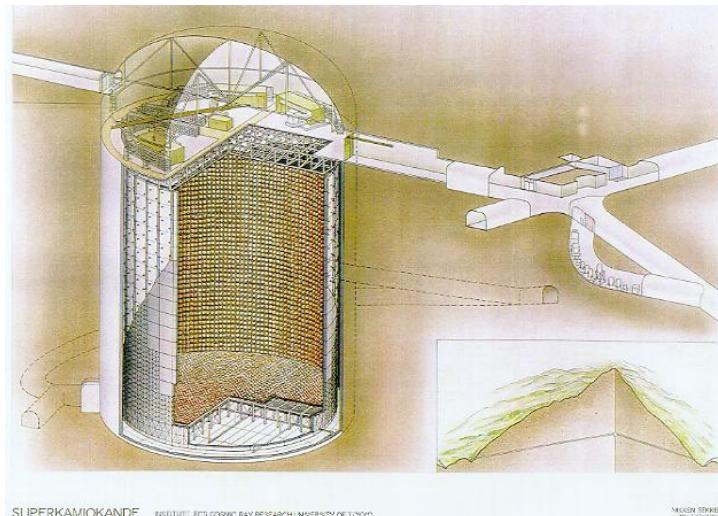
Upward  $\nu_\mu \rightarrow \mu$   
How does the astro spectrum continue below 100 TeV?

# Outline

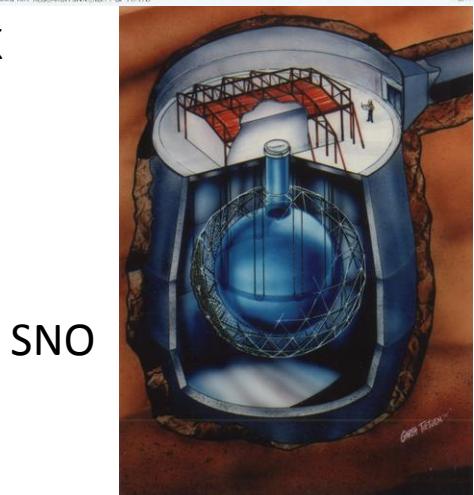
- Historical introduction
  - Calculating the flux of atmospheric  $\mu$  and  $\nu$
- Muon charge ratio,  $K/\pi$  ratio,  $\nu/\bar{\nu}$  ratio
- Atmospheric neutrinos to PeV
  - Energy dependence of hadron production
  - Must account for knee in cosmic-ray spectrum
  - Prompt neutrinos from charm decay
- Atmospheric neutrino self-veto
- Atmospheric  $\nu$  backgrounds in IceCube

# Detecting neutrinos in H<sub>2</sub>O

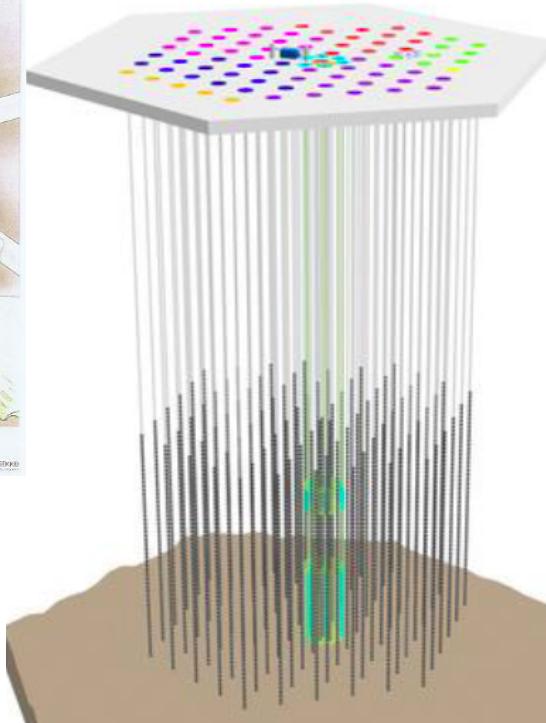
*Proposed by Greisen, Reines, Markov in 1960*



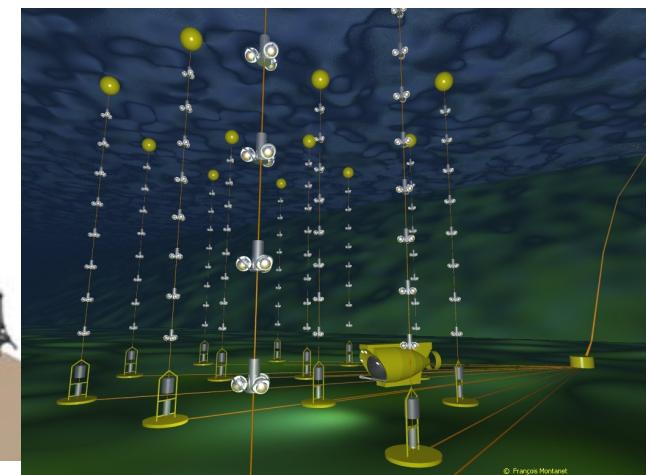
Super-K



SNO



IceCube



ANTARES

## Heritage:

- DUMAND
- IMB
- Kamiokande
- Baikal
- AMANDA

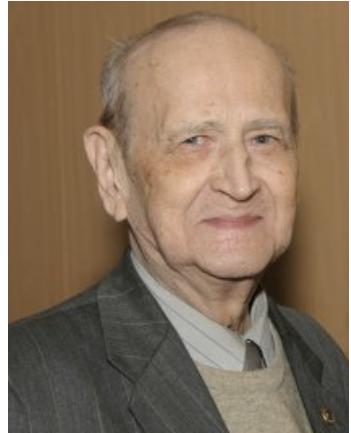
# 1961

SOVIET PHYSICS JETP

VOLUME 12, NUMBER 6

JUNE, 1961

*ANGULAR DISTRIBUTIONS OF HIGH-ENERGY MUONS IN THE ATMOSPHERE AND  
THEIR PRODUCTION MECHANISM*



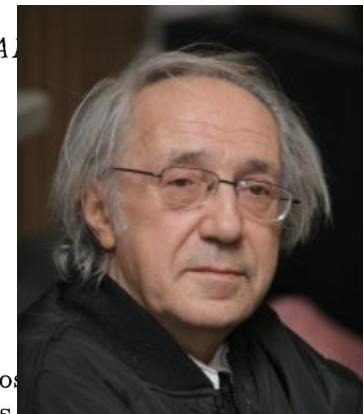
G. T. ZATSEPIN and V. A. KUZ'MIN

P. N. Lebedev Physics Institute, Academy of Sciences, U.S.S.R.

Submitted to JETP editor July 10, 1960

J. Exptl. Theoret. Phys. (U.S.S.R.) **39**, 1677-1685 (December, 1960)

The kinetic equation for  $\mu$  mesons in the atmosphere in which the decay and energy losses are taken into account is solved. The angular distributions of  $10^{11} - 10^{14}$  ev  $\mu$  mesons in the atmosphere are computed for two possible production mechanisms:  $\pi \rightarrow \mu + \nu$  and  $K \rightarrow \mu + \nu$  decays. The results indicate that in the energy range of  $10^{11} - 5 \times 10^{12}$  ev the  $\mu$ -meson angular distributions depend significantly on the mechanism of their production.



K

SOVIET PHYSICS JETP

VOLUME 14, NUMBER 6

JUNE,

*NEUTRINO PRODUCTION IN THE ATMOSPHERE*

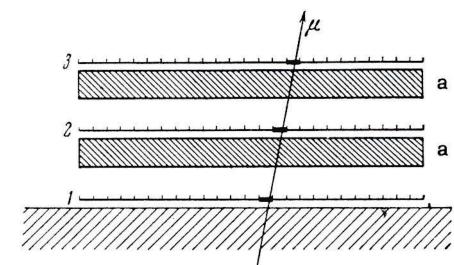
G. T. ZATSEPIN and V. A. KUZ'MIN

P. N. Lebedev Physics Institute, Academy of Sciences, U.S.S.R.

Submitted to JETP editor March 8, 1961

J. Exptl. Theoret. Phys. (U.S.S.R.) **41**, 1818-1827 (December, 1961)

The energy spectra and angular distribution of neutrinos produced in the atmosphere in the  $\pi \rightarrow \mu + \nu$  and  $\mu \rightarrow e + \nu + \bar{\nu}$  decays are calculated taking the  $\mu$ -meson energy losses at neutrino energies  $\varepsilon = 10^9 - 3 \times 10^{11}$  ev into account. It is shown that the neutrino flux from the  $\mu \rightarrow e + \nu + \bar{\nu}$  decay is comparable with that from the  $\pi \rightarrow \mu + \nu$  decay.  $\mu$ -meson energy losses only weakly affect neutrino production. K mesons produce neutrinos more efficiently than do  $\pi$  mesons. An experimental arrangement for detecting high-energy cosmic ray neutrinos is proposed.



# Calculating atmospheric lepton fluxes: two approaches

1. Analytic/numerical solutions of the cascade equations

$$\begin{aligned} \frac{dN_i(E_i, X)}{dX} = & -\frac{N_i(E_i, X)}{\lambda_i} - \frac{N_i(E_i, X)}{d_i} \\ & + \sum_{j=i}^J \int_E^\infty \frac{F_{ji}(E_i, E_j)}{E_i} \frac{N_j(E_j, X)}{\lambda_j} dE_j \end{aligned}$$

2. Convolve primary spectrum with yields per primary

$$\phi_\nu(E_\nu, \theta) = \sum_A \int_{E_\nu}^\infty \phi_A(E_A) Y_\nu(A, E_\nu, E_A, \theta) dE_A,$$

# Scaling/power-law solutions for $\nu$

Same form for  $\mu$ ;  
Different kinematics  
 $\rightarrow \mu, \nu$  differences

$$A_{i\nu} = \frac{Z_{Ni} \times BR_{i\nu} \times Z_{i\nu}}{1 - Z_{NN}}$$

$$Z_{\pi\mu} = \frac{1 - r_\pi^{\gamma+1}}{(\gamma + 1)(1 - r_\pi)} \text{ and } \frac{\epsilon_\pi}{\cos \theta E_\mu} \frac{1 - r_\pi^{\gamma+2}}{(\gamma + 2)(1 - r_\pi)}$$

$$Z_{\pi\nu} = \frac{(1 - r_\pi)^\gamma}{(\gamma + 1)} \text{ and } \frac{\epsilon_\pi}{\cos \theta E_\mu} \frac{(1 - r_\pi)^{(\gamma+1)}}{(\gamma + 2)}$$

$$\begin{aligned} \phi_\nu(E_\nu) &= \phi_N(E_\nu) \\ &\times \left\{ \frac{A_{\pi\nu}}{1 + B_{\pi\nu} \cos(\theta) E_\nu / \epsilon_\pi} + \frac{A_{K\nu}}{1 + B_{K\nu} \cos(\theta) E_\nu / \epsilon_K} \right. \\ &\quad \left. + \frac{A_{\text{charm}\nu}}{1 + B_{\text{charm}\nu} \cos(\theta) E_\nu / \epsilon_{\text{charm}}} \right\}, \end{aligned}$$

$$\begin{aligned} \epsilon_\pi &= 115 \text{ GeV} \\ \epsilon_K &= 850 \text{ GeV} \\ \epsilon_{\text{charm}} &> 10 \text{ PeV} \end{aligned}$$

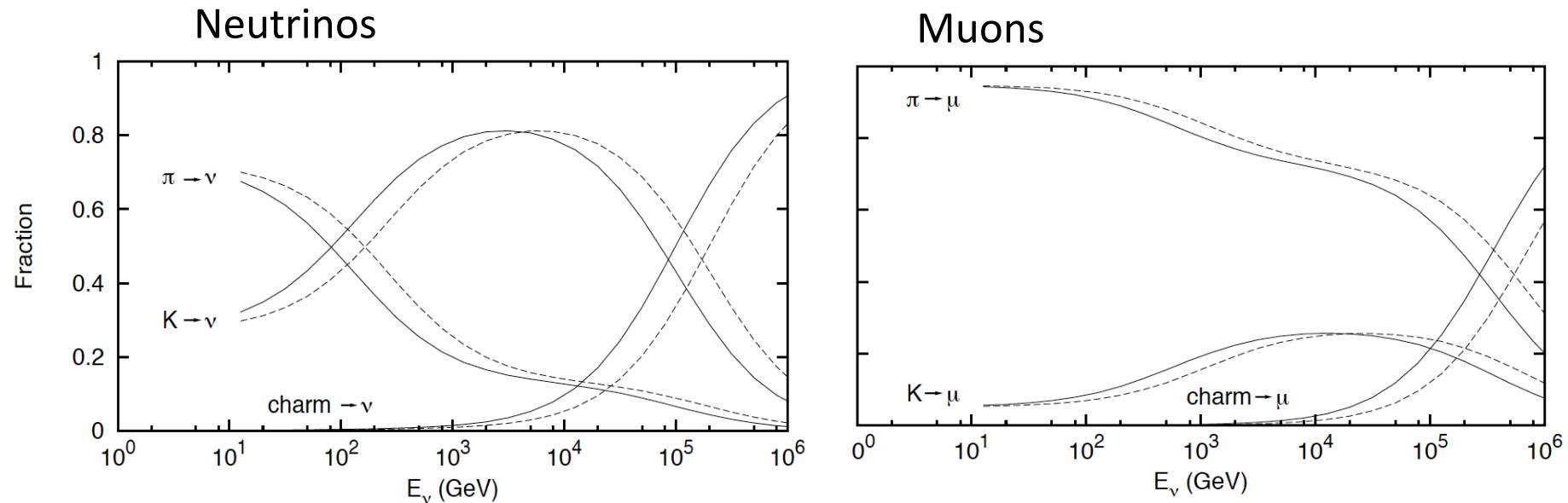
$$Z_{pK^+} = \frac{1}{\sigma} \int x^\gamma \frac{d\sigma(x)}{dx} dx$$

Spectral index  
 $\gamma + 1 \approx 2.7$

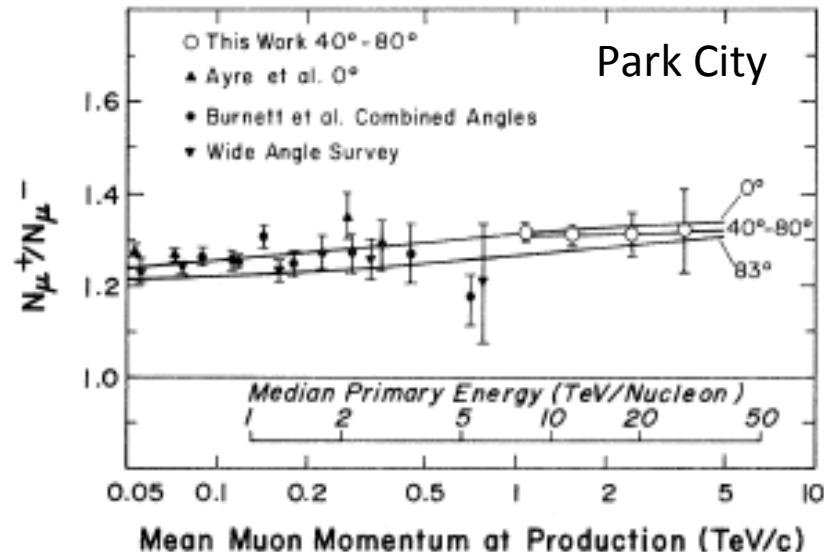
$$\begin{aligned} r_\pi &= 0.573 \text{ but} \\ r_K &= 0.0458 \end{aligned}$$

# Importance of kaons for neutrinos

- Atmospheric  $\nu_\mu$  mainly from  $K^{+/-}$
- TeV atmospheric  $\nu_e$  from  $K_{e3}$  decays of  $K^0, K^{+/-}$
- Associated production ( $p \rightarrow K^+ \Lambda$ ) favors  $K^+$
- Charm  $\rightarrow \mu, \nu$  : small but potentially important at high E
  - contribution isotropic (compared to secant  $\theta$  effect for >TeV leptons from decay of  $\pi$  and  $K$ )

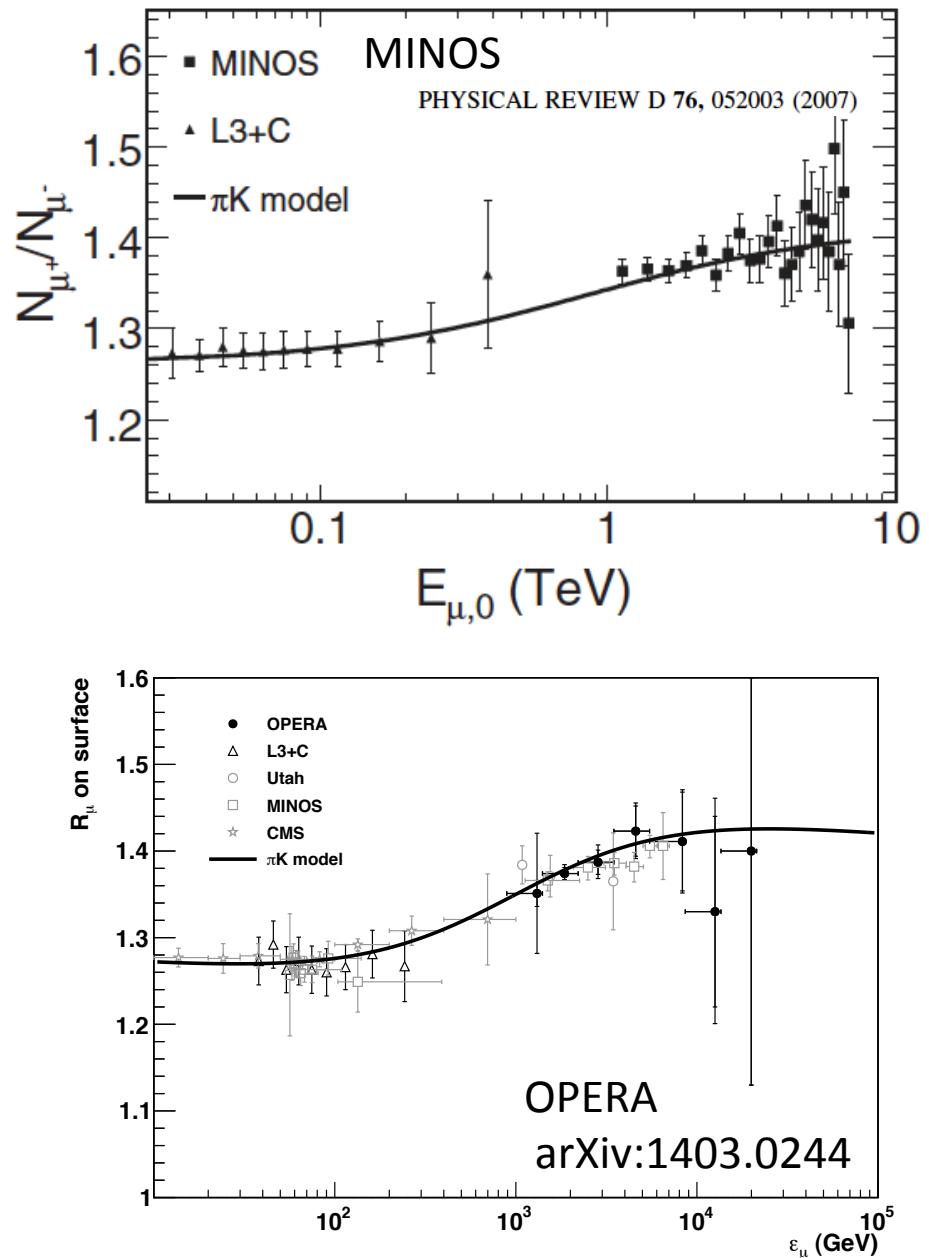


# Muon charge ratio



Ashley, Elbert, Keuffel, Larsen, Morrison, PRL 31(1973) 1091

- Ratio due to excess of p over n in primary CR + steep spectrum which favors  $p \rightarrow \pi^+$  over  $p \rightarrow \pi^-$
- Rise at TeV due to increased importance of Kaons (especially  $K^+$ )



# Muon charge ratio including kaons

$$\frac{\mu^+}{\mu^-} = \left[ \frac{f_{\pi^+}}{1 + B_{\pi\mu} \cos(\theta) E_\mu / \epsilon_\pi} + \frac{\frac{1}{2}(1 + \alpha_K \beta \delta_0) A_{K\mu} / A_{\pi\mu}}{1 + B_{K\mu}^+ \cos(\theta) E_\mu / \epsilon_K} \right] \\ \times \left[ \frac{(1 - f_{\pi^+})}{1 + B_{\pi\mu} \cos(\theta) E_\mu / \epsilon_\pi} + \frac{(Z_{NK^-}/Z_{NK}) A_{K\mu} / A_{\pi\mu}}{1 + B_{K\mu} \cos(\theta) E_\mu / \epsilon_K} \right]^{-1}$$

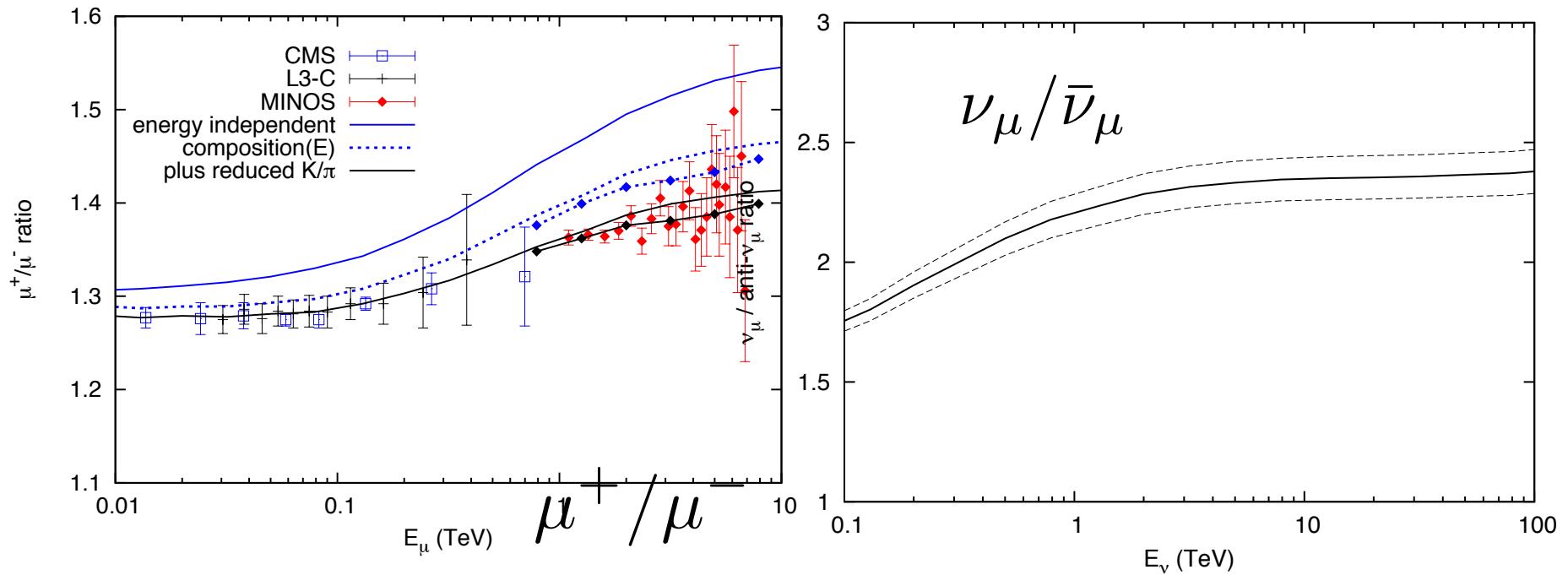
where  $\alpha_K = \frac{Z_{pK^+} - Z_{pK^-}}{Z_{pK^+} + Z_{pK^-}}$

TG, Astropart. Phys. 35 (2012) 801

OPERA fit data as a function of  $\cos\theta$  and  $E$  with two free parameters.  
They find  $Z_{pK^+} = 0.0086 \pm 0.0004$  and  $\delta_0 = 0.61$  at  $\sim 20$  TeV/nucleon

# Results for $Z_{pK^+} = 0.086 \pm 0.04$

$p \rightarrow \Lambda K^+$  is relatively more important for  $\nu/\bar{\nu}$

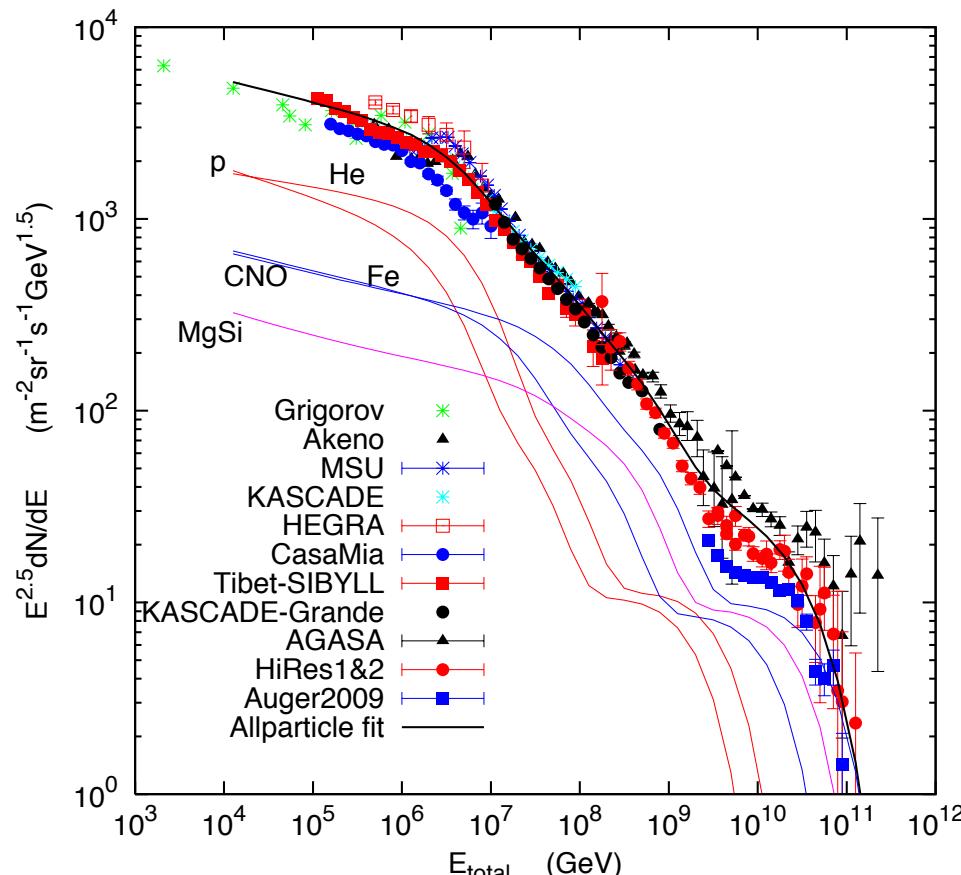


Important because  $\sigma_\nu \neq \sigma_{\bar{\nu}}$

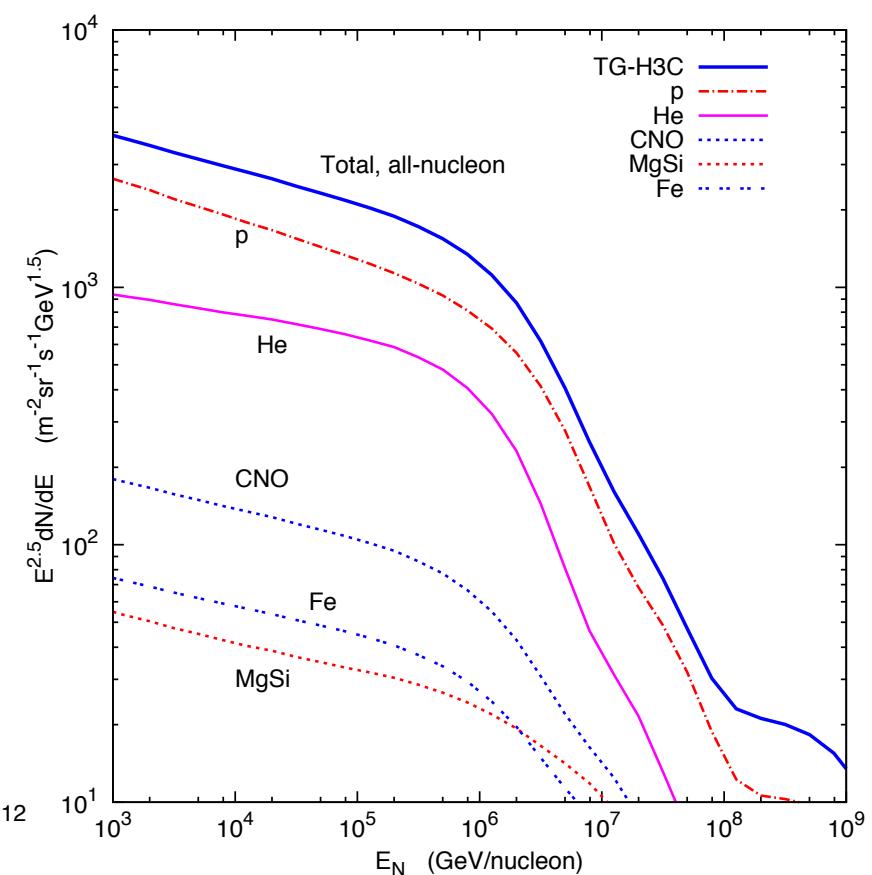
# Primary spectrum

- Combine information
  - from direct measurements < 100 TeV
  - with air shower measurements of all-particle spectrum at higher E
- Assumptions:
  - 5 nuclear groups: p, He, CNO, Mg-Si, Fe
  - 3 populations: SNR, Hillas' Galactic component B, extra-galactic
  - All features depend on rigidity,  $R = P_c / Ze$
  - All particle spectrum:  $\phi_i(E) = \sum_{j=1}^3 a_{i,j} E^{-\gamma_{i,j}} \times \exp\left[-\frac{E}{Z_i R_{c,j}}\right]$
  - Spectrum of nucleons:  $\phi_{i,N}(E_N) = A \times \phi_i(A E_N)$
- Requirements
  - Consistency with air shower measurements of the all-particle spectrum
  - Anchor to composition from direct experiments below 100 TeV

# Spectrum of nucleons determines fluxes of atmospheric $\nu$ and $\mu$

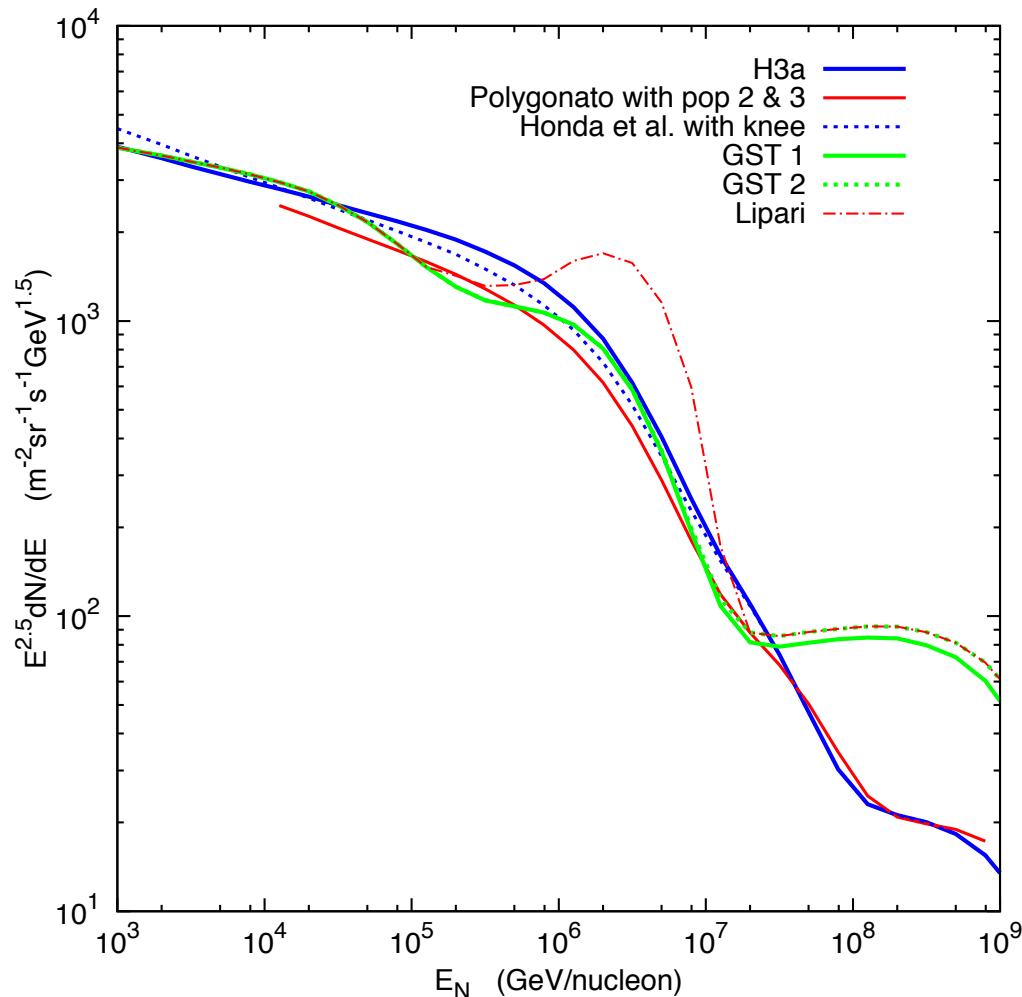


All-particle spectrum



Spectrum of nucleons

# Spectrum of nucleons



## Challenge:

For the first time, we must account for the knee in the cosmic-ray spectrum to calculate atmospheric neutrinos

Also need to account for non-scaling behavior of meson production over wide energy range

# Atmospheric neutrinos to PeV

- Bartol fluxes,                    Honda et al.
  - G. Barr et al. PRD 70, 023006; Honda et al., [PRD 75 \(2007\) 043006](#)
  - Full Monte Carlo gives yields for a grid of primary energies and masses
  - Convolve with primary spectrum
  - Produce tables of neutrino fluxes to 10 TeV
- Full Monte Carlo calculations
  - are awkward at high energy because
  - mesons almost always interact rather than decay
- Use numerical method:
  - Thunman, Ingelman, Gondolo, Astropart. Phys. 5 (1996) 309

# Unified approach to calculating $\phi_\nu(E_\nu)$

- Use simple equations

$$A_{i\nu} = \frac{Z_{Ni} \times BR_{i\nu} \times Z_{i\nu}}{1 - Z_{NN}}$$

$$\phi_\nu(E_\nu) = \phi_N(E_\nu) \times \sum_{i=1,3} \left( \frac{A_{i\nu}}{1 + B_{i\nu} \cos^* \theta E_\nu / \epsilon_i} \right)$$

- With energy-dependent Z-factors

$$Z_{i,j}(E) = \int_E^\infty dE' \frac{\phi_N(E')}{\phi_N(E)} \frac{dn_{i,j}(E', E)}{dE}$$

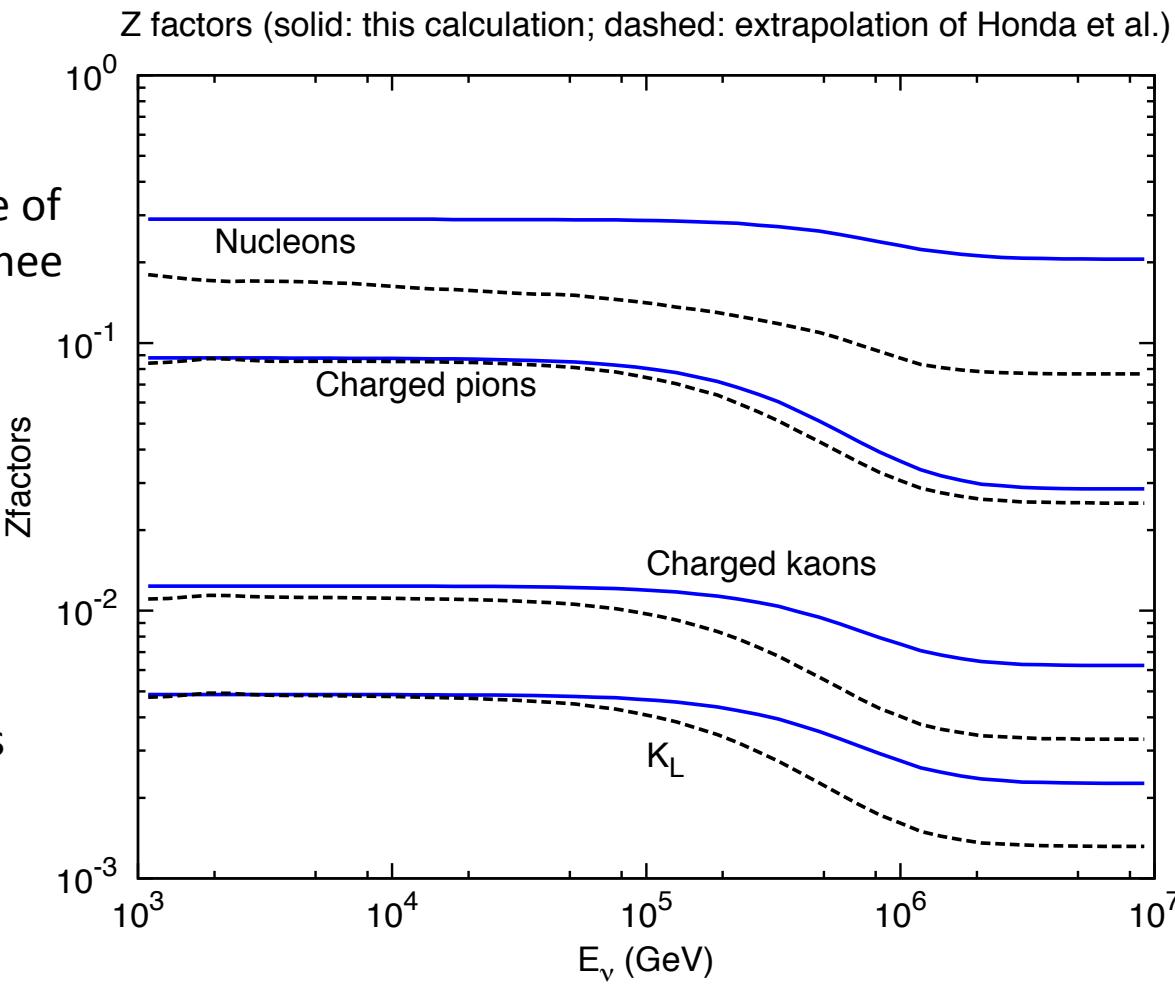
- Allows systematic evaluation of
  - Different primary spectrum/composition models
  - Uncertainties in hadronic interactions
  - Non-scaling, non-power-law energy dependence

# Energy-dependent Z-factors

Solid lines:  
Energy-independent  
interactions; only source of  
energy dependence is knee

Dotted lines:  
thanks to M. Honda for  
providing extended  
table of Z-factors from  
PRD 75 (2007) 043006

Monte Carlo calculations  
of atmospheric  $\nu$  extend  
only to 10 TeV (also for  
“Bartol” fluxes, 2004:  
G. Barr et al. PRD 70, 023006



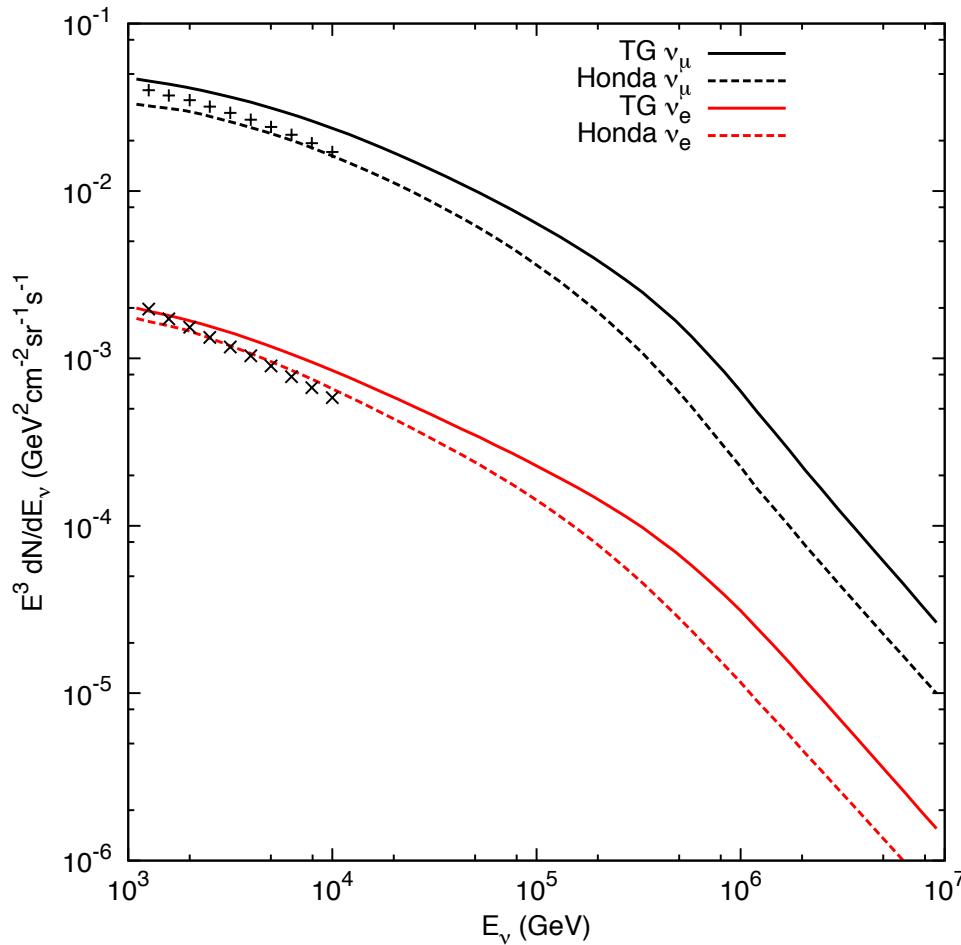
# Compare with extrapolated Honda

Solid lines: energy-independent hadronic interactions.

Dotted lines: Honda et al with same primary spectrum

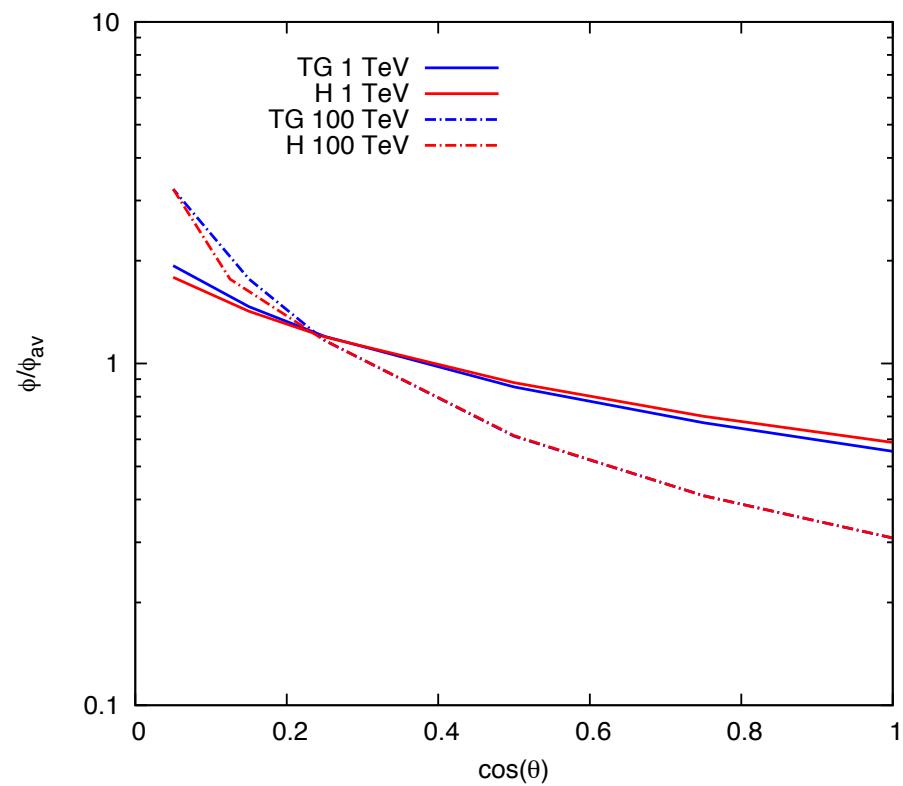
Data points from Honda et al. Monte Carlo calculation, which is steeper at low energy due to neutrinos from muon decay. Also, it has a slightly different primary spectrum.

Note:  $\nu_e$  are from  $\text{Ke}^3$  decays, including  $7 \cdot 10^{-4} K_S$ , which becomes significant only for Energy  $\sim \varepsilon_{\text{critical}} \approx 120 \text{ TeV}$ .  
TG & S. Klein, arXiv:1409.4924

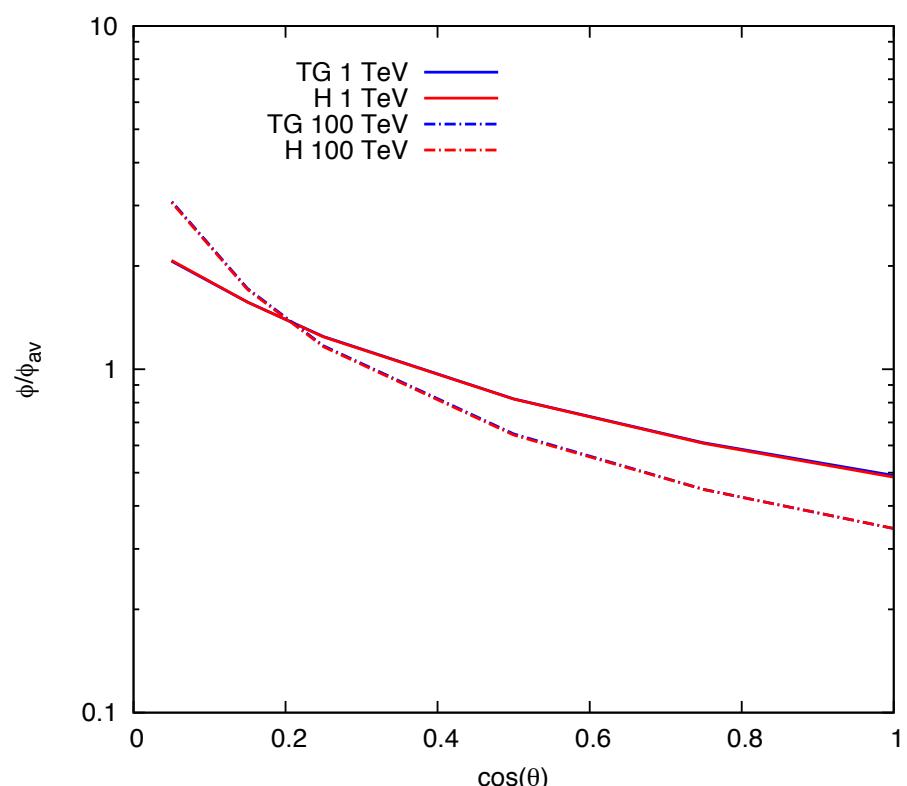


# Angular distributions

angular-numu

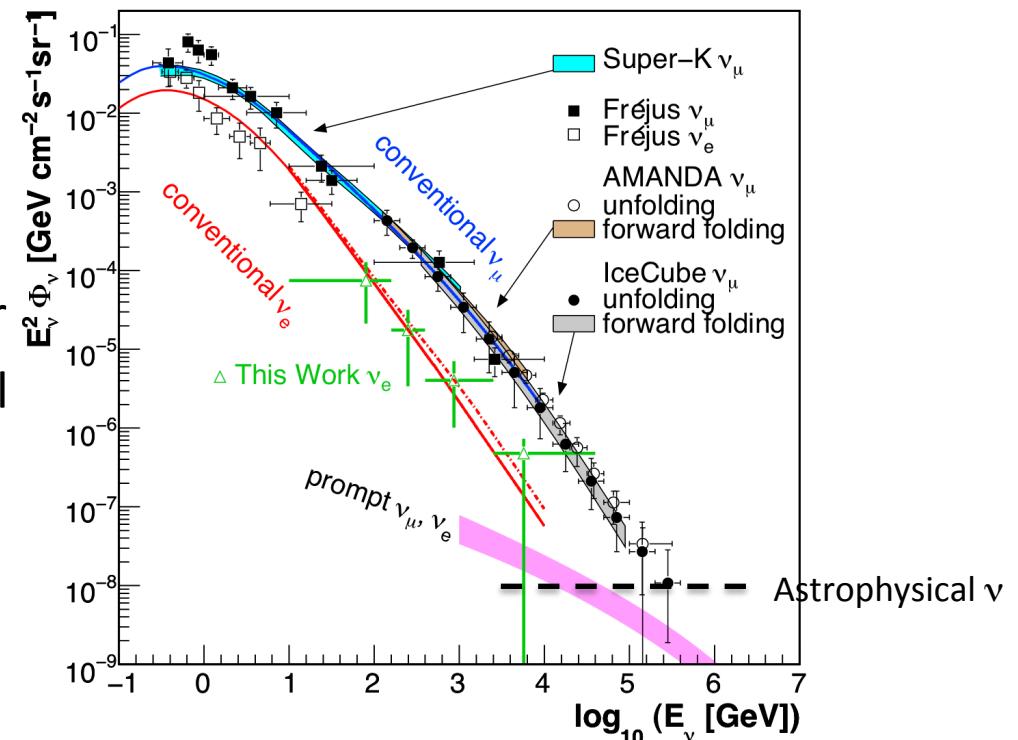


angular-nue



# Importance of charm

- Critical energy  $\epsilon_{\text{charm}} \approx 10^7$  GeV
- So spectrum of  $\nu$  from charm follows primary spectrum
- Conventional  $\nu$  one power steeper
- Crossover of prompt/conventional competes with the transition to astrophysical neutrinos
- A charmed analog of  $p \rightarrow K^+ \Lambda$  may be important

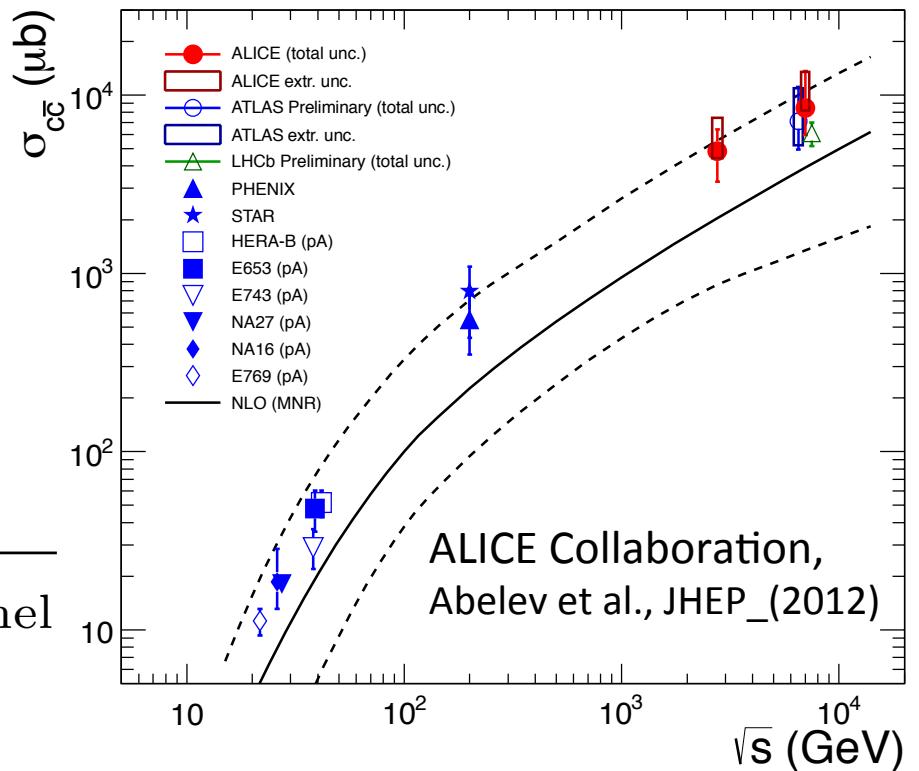


# Estimate prompt $\nu$ from charm:

- Scale inclusive cross sections from plot
  - Limited phase space:
  - Use FONLL to get total  $\sigma_{\text{charm}}$
  - Compare inclusive  $\sigma_\pi$ :

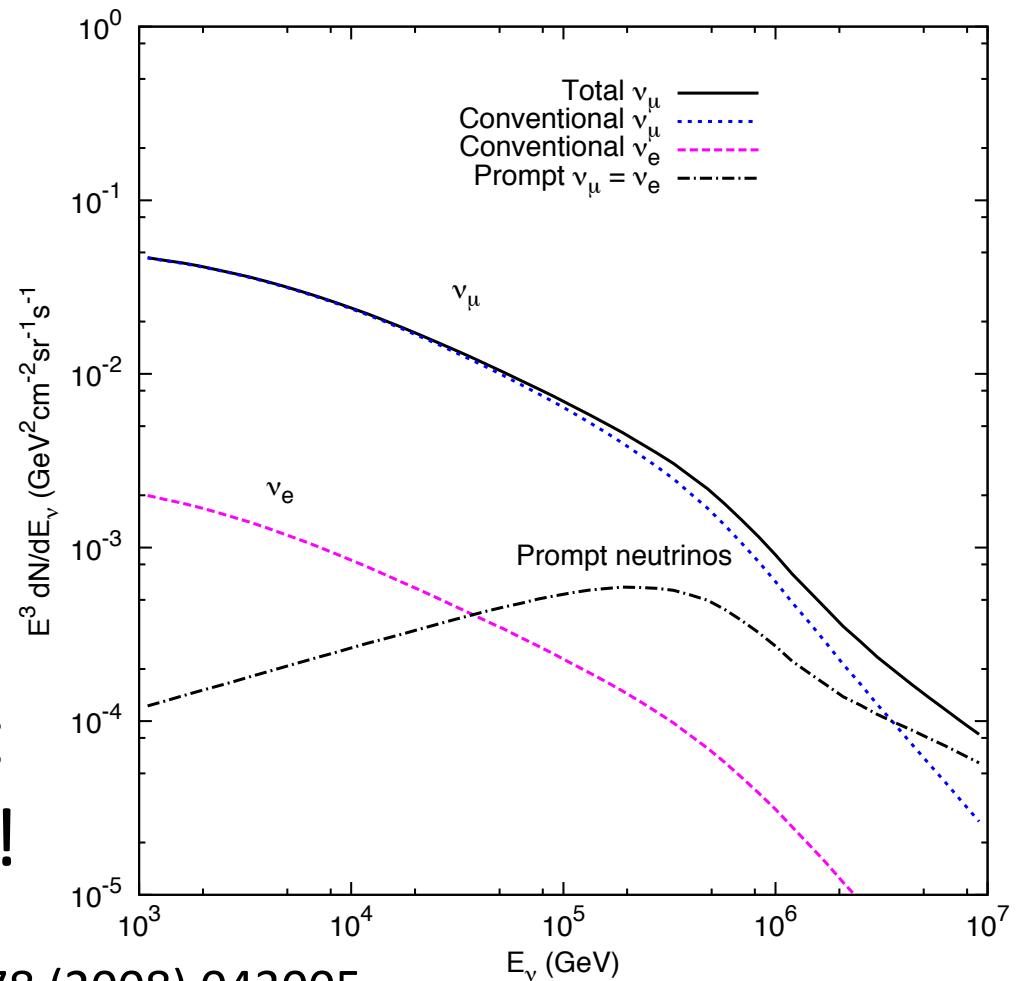
$$Z_{N \text{ charm}} \sim Z_{N\pi} \frac{\sigma_{\text{charm}}}{\langle n_\pi \rangle \sigma_{\text{inel}}}$$

- Add charm decay kinematics and nuclear target effect



# Prompt vs conventional neutrinos

- Estimate  $\approx$  ERS\*
- For conventional  $\nu$  (for  $E >$  TeV)  
 $\phi(\nu_e) \approx \phi(\nu_\mu)/20$
- Prompt crossover earlier for  $\nu_e$
- Prompt component cannot be neglected!

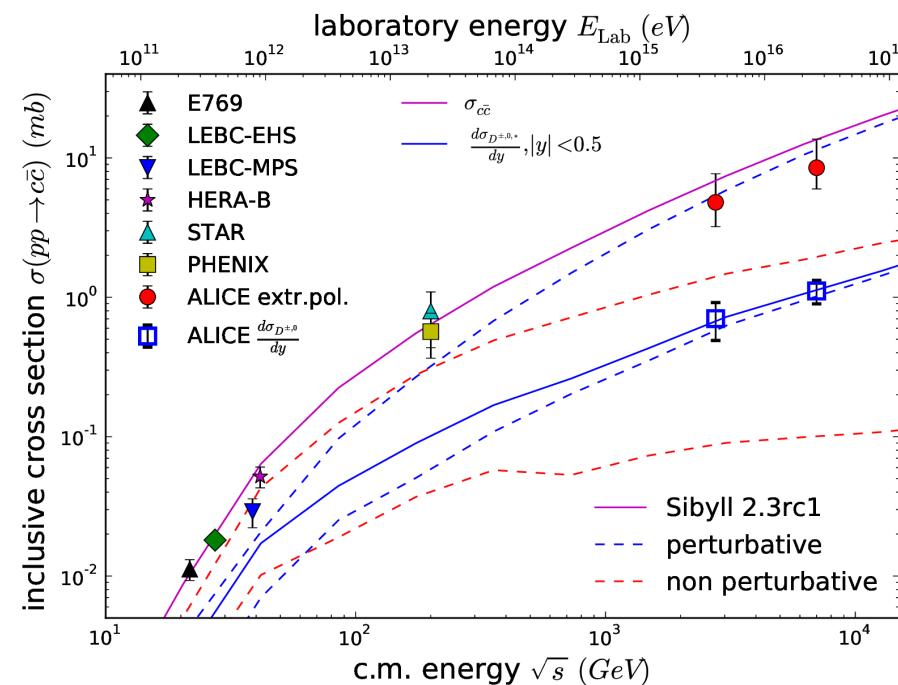


\*ERS = Enberg, Reno, Sarcevic, PRD 78 (2008) 043005

# Adding charm to SIBYLL (post-LHC)

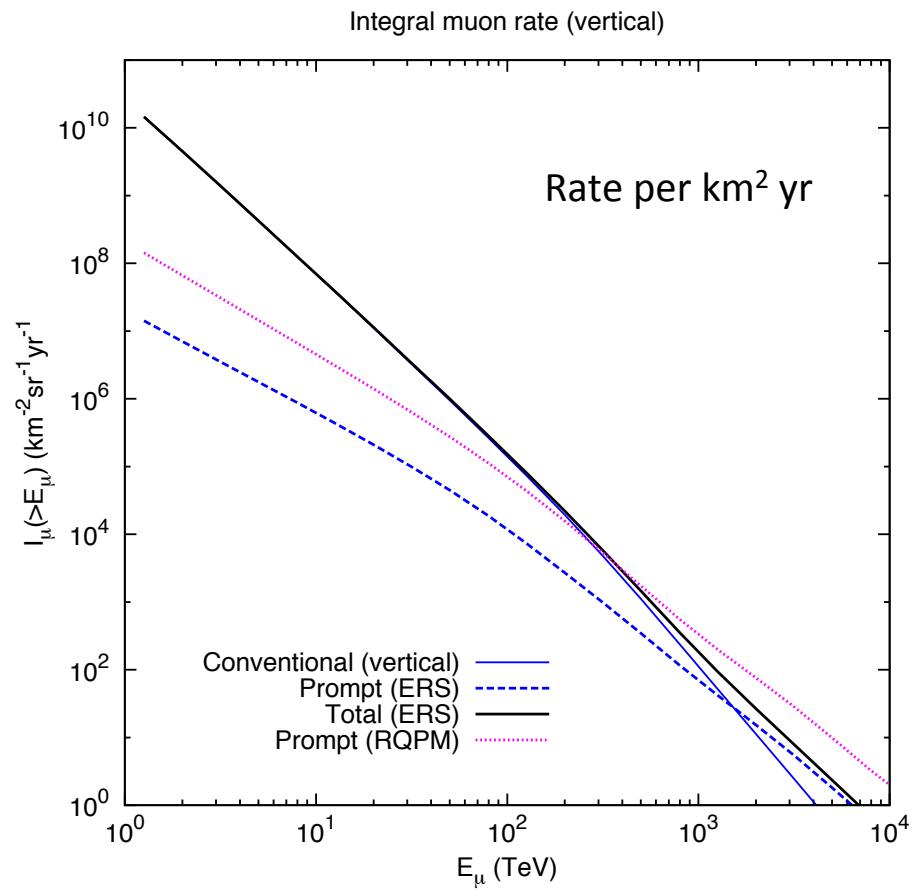
Felix Riehn, ISVHECRI 2014

Strategy: add charm production including a non-perturbative component adjusted to reproduce fixed target measurements in addition to the perturbative QCD contribution



# Can we identify prompt component with atmospheric muons?

- Advantages:
  - No astro component
  - High rate
  - Angular dependence
    - Isotropic for prompt
    - $\sec(\theta)$  for conventional
  - Seasonal variation\*
  - Strong for conventional
  - Absent for prompt
- Problems in practice
  - Crossover at high energy
  - Energy resolution



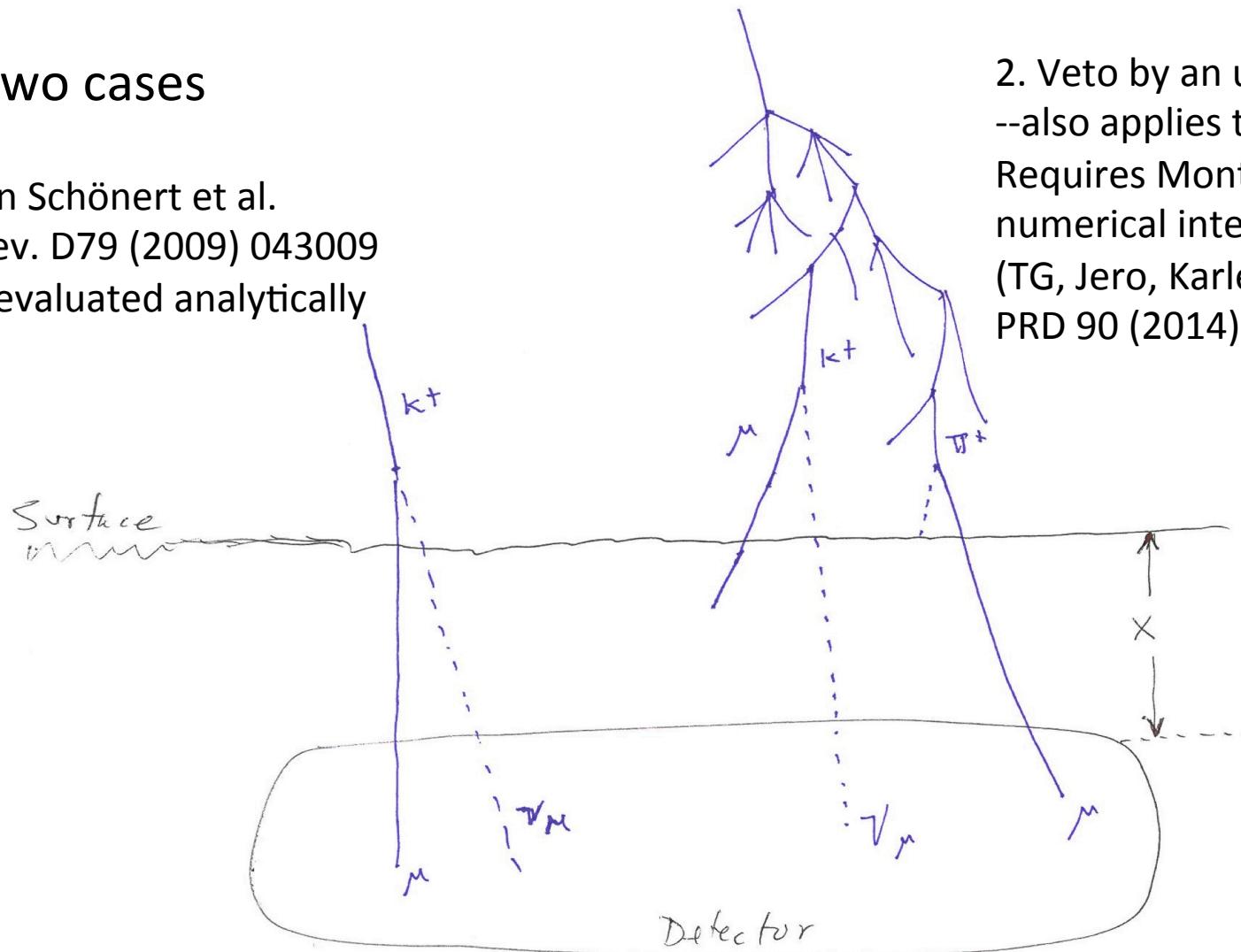
\*P. Desiati & TG, PRL 105 (2010) 121102

# Atmospheric neutrino self veto

Two cases

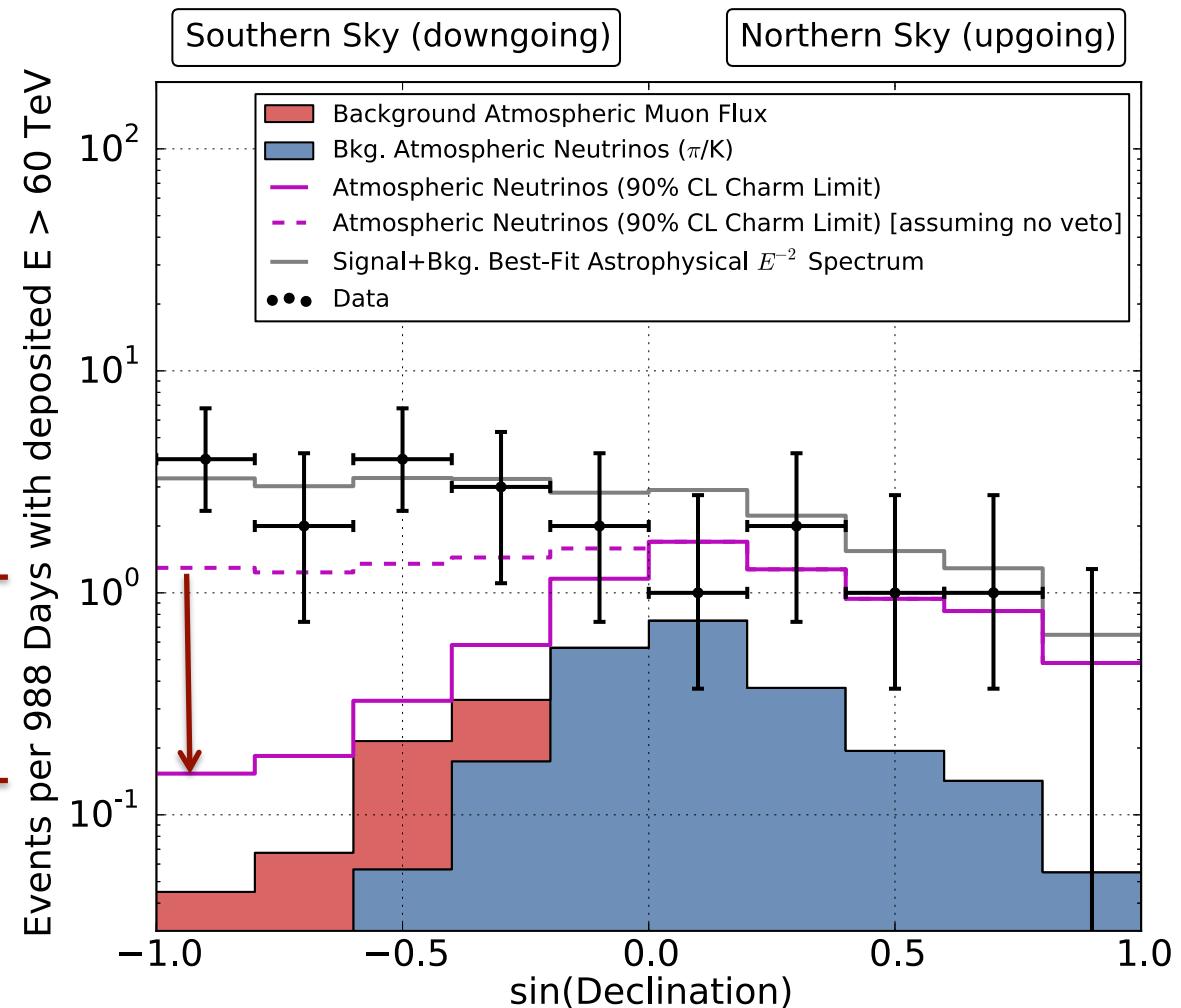
1. Stefan Schönert et al.  
Phys. Rev. D79 (2009) 043009  
Can be evaluated analytically

2. Veto by an unrelated  $\mu$   
--also applies to  $\nu_e$   
Requires Monte Carlo or  
numerical integration  
(TG, Jero, Karle, van Santen  
PRD 90 (2014) 023009)



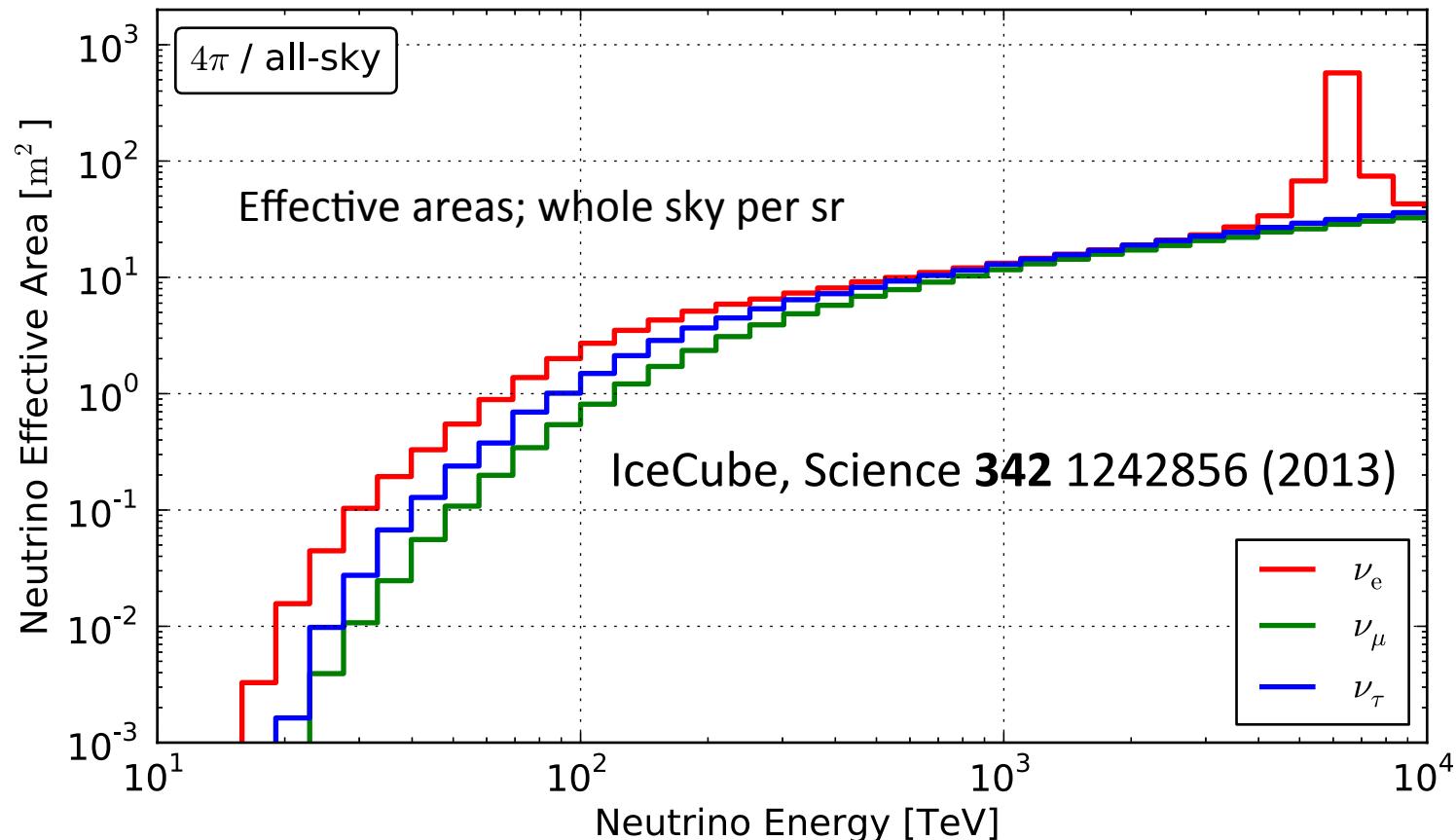
# Angular distribution ( $E > 60$ TeV)

Atmospheric  $\nu$  veto



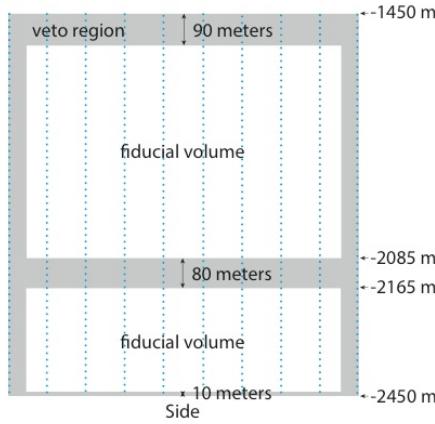
Note shape of prompt atmospheric  $\nu$  background:  
Veto does not have to be complete to be useful

# Fold fluxes with IceCube $A_{\text{eff}}$ to get rates

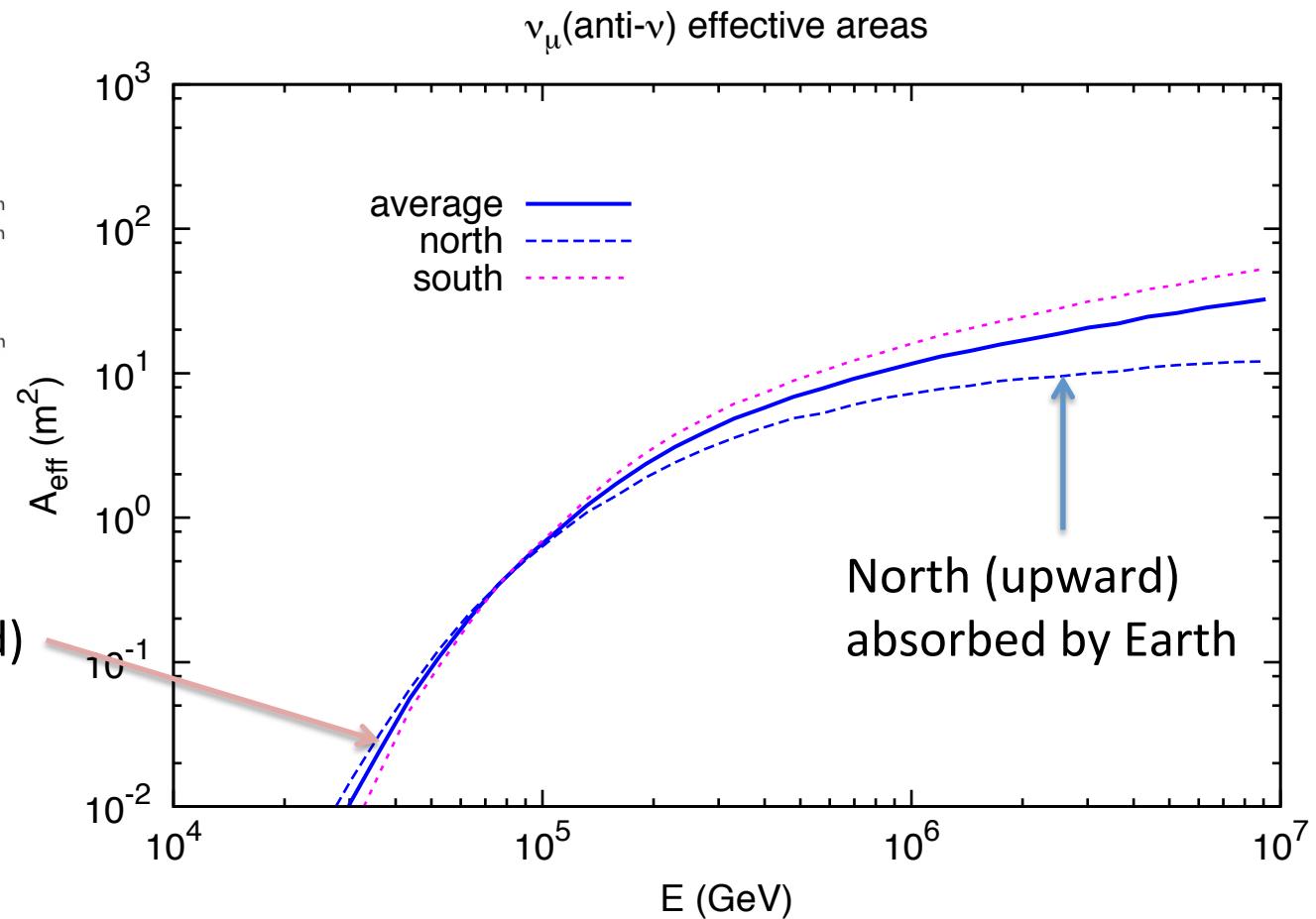


Visible energy threshold suppresses  $\nu_\tau$  and  $\nu_\mu$  relative to  $\nu_e$

# IceCube $\nu_\mu$ effective areas separated by hemisphere



Veto tighter for  
South (downward)  
than for North



# Application to IceCube

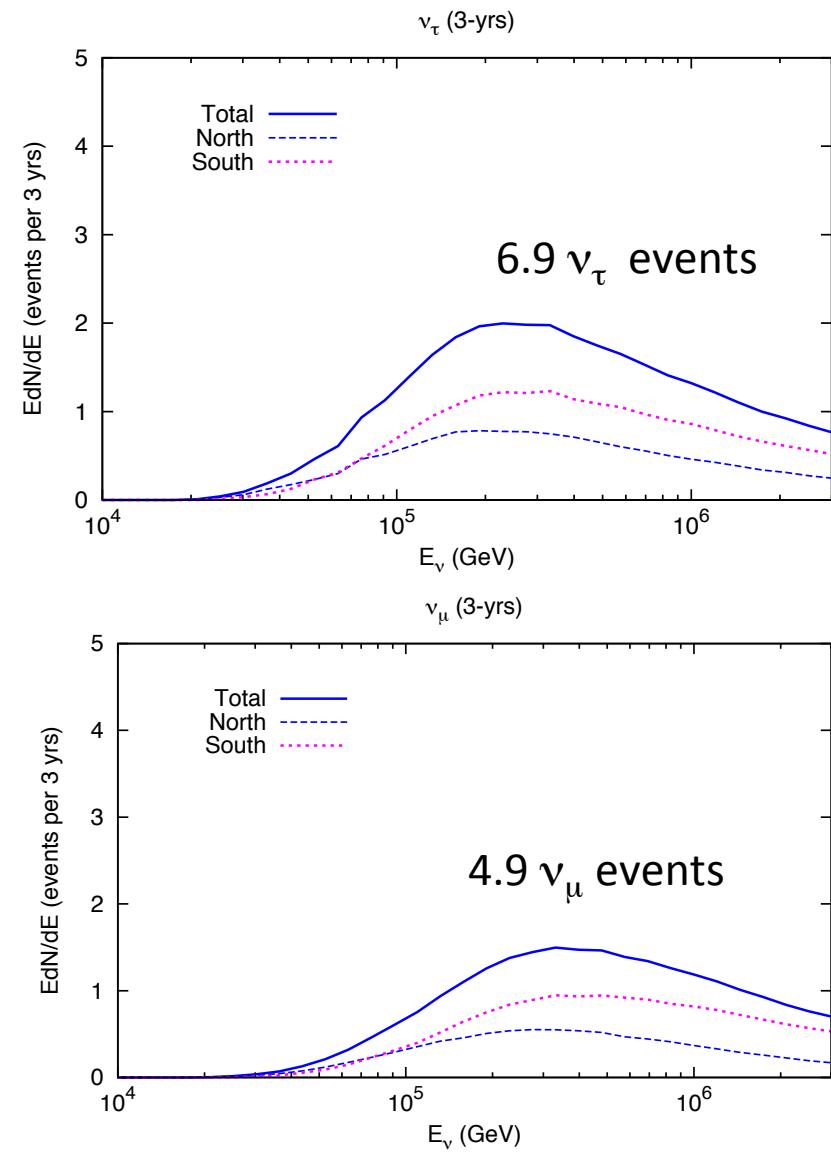
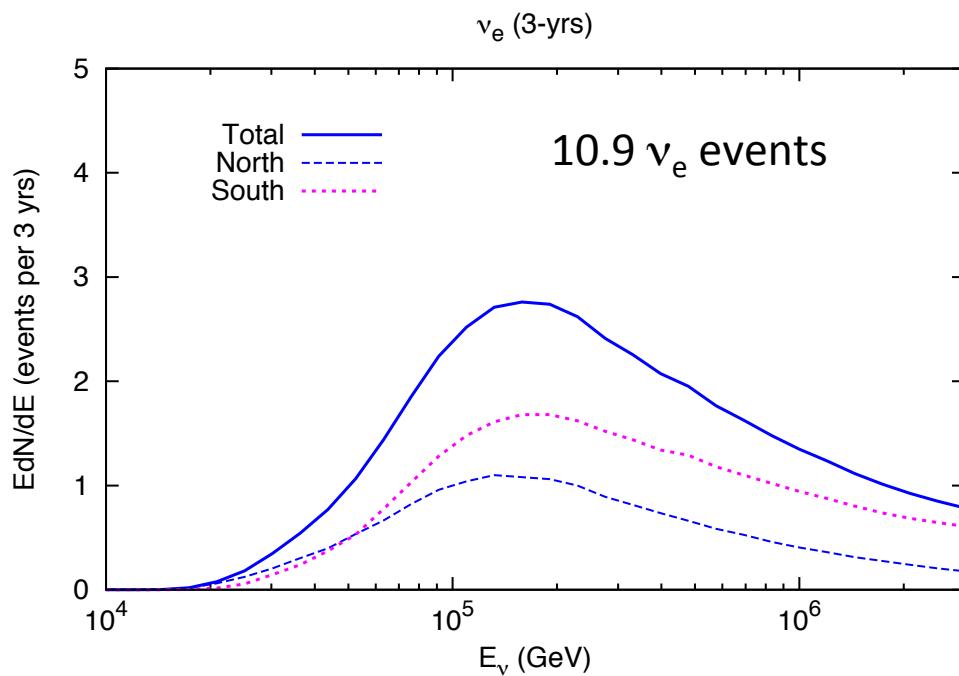
- IceCube 3 yr analysis suggests two fits for astrophysical component up to 3 PeV:

$$E_\nu^2 \phi_\nu = 0.95 \times 10^{-8} \frac{\text{GeV}}{\text{cm}^2 \text{sr s}} \text{ per flavor}$$

$$E_\nu^2 \phi_\nu = 1.5 \times 10^{-8} \left( \frac{E}{100\text{TeV}} \right)^{-0.3} \frac{\text{GeV}}{\text{cm}^2 \text{sr s}} \text{ per flavor}$$

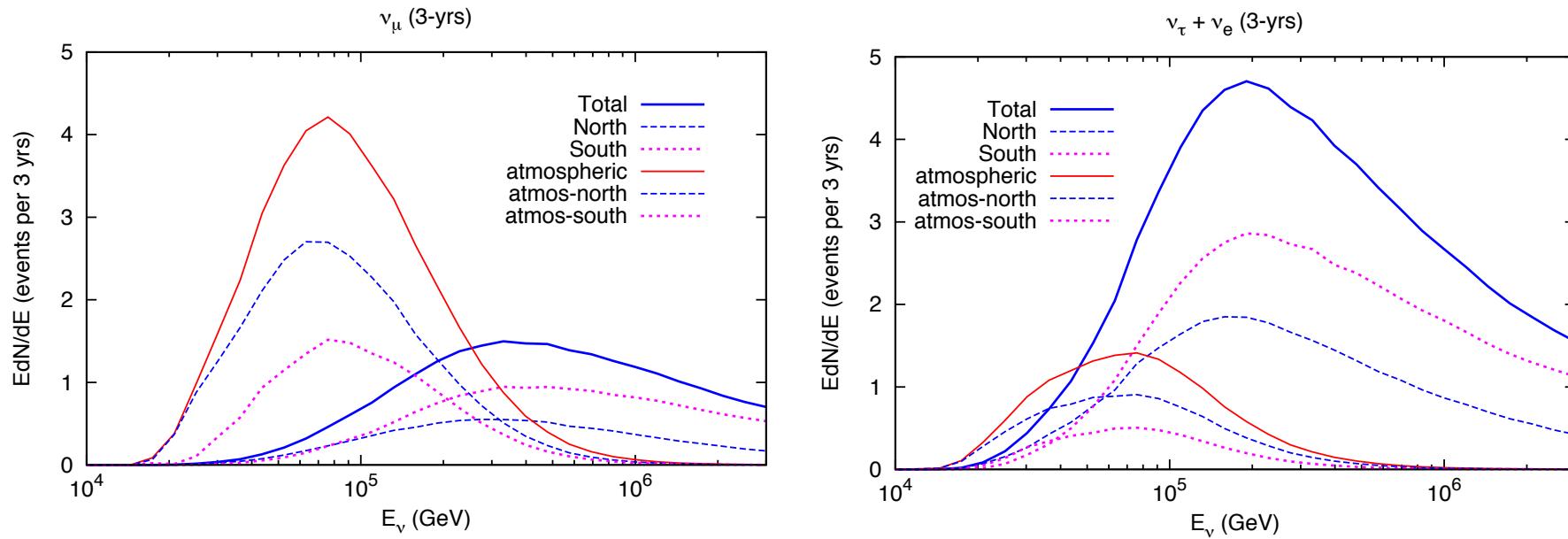
# Astrophysical events for $E^{-2.3}$ fit

(Convolve astro spectrum with Aeff)



Note: Plots are vs  $\nu$  energy (not  $E_{\text{vis}}$ )  
assuming  $\phi_\nu \sim (E_\nu)^{-2}$

# Signal/background

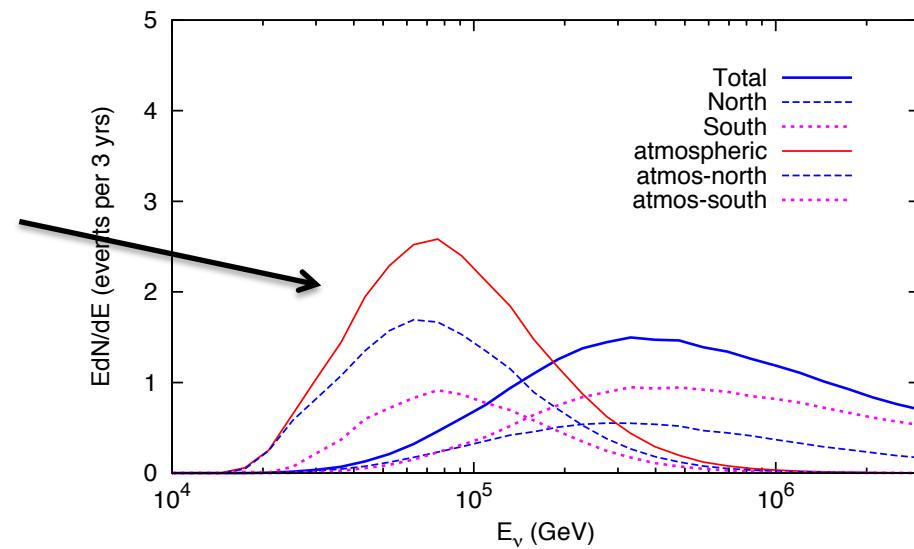
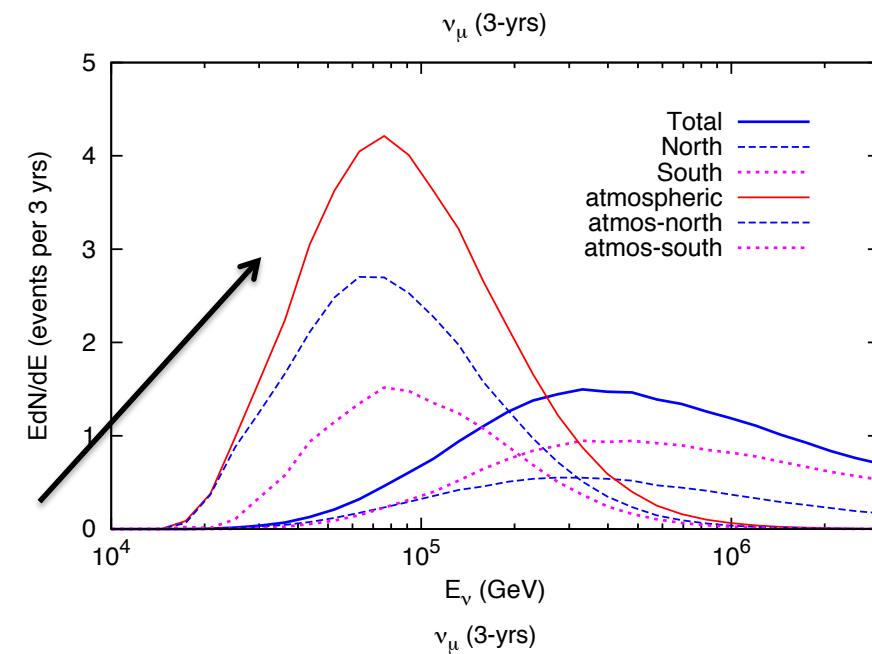


Note: plots are vs true neutrino energy, not  $E_{\text{visible}}$   
The distortion is biggest for  $\nu_\mu$

# Uncertainty in background limits inference on flavor ratio at Earth

Scaling extrapolation with knee:  
expect 7 atmospheric  $\nu_\mu$  in 3 yrs  
IceCube HESE analysis

Extrapolation of Honda flux  
(with knee):  
Expect  $\approx 4$  atmospheric  $\nu_\mu$



# 37 events assuming $E^{-2.3}$ spectrum

TABLE III. Accounting for thirty-seven events ( $E^{-2.3}$  spectrum)

	South (before selfveto)	North	Total	Cascades	Tracks
Astro $\nu_e$	6.94	N/A	3.94 10.88		
Astro $\nu_\tau$	4.13	N/A	2.80 6.93	18	5
Astro $\nu_\mu$	3.04	N/A	1.83 4.87		
Total Astro	14.1	N/A	8.6 22.7		
Conventional $\nu_e$	0.53	(0.69)	0.68 1.21		
Conventional $\nu_\mu$	2.53	(4.58)	4.62 7.15	4	6
Charm (ERS) $\nu_e$	0.36	(1.40)	1.12 1.48		
Charm (ERS) $\nu_\mu$	0.10	(0.46)	0.37 0.47		
Total atmospheric	3.52	(7.013)	6.79 10.3		
Total neutrinos	17.6	(21.2)	15.4 33		
Atmospheric $\mu$ (by subtraction)	$\approx 4$	N/A	0 $\approx 4$		4?
				22	15
Data:	28				9

# Summary comments

- Analytic/numerical evaluation of  $\nu$  fluxes
  - Account for non-scaling, and knee of spectrum
  - Useful for exploring uncertainties in atmospheric  $\nu$  flux
- Kaon channel dominates atmospheric  $\nu$ 
  - Increase of  $\mu^+/\mu^-$  sets level of kaon production
  - Implications for  $\nu/\bar{\nu}$  ratio and rate of atmospheric background
- Level of charm production is still uncertain
  - Selex expt suggests some intrinsic charm
  - Hidden in IceCube  $\nu$  by astrophysical component
  - Sibyll with charm should be ready soon
- $\nu$  self-veto reduces downward background atmospheric  $\nu$
- Cascade/track and flavor ratio:
  - more data + better understanding of background needed

# Discussion

- Physics motivation:
  - Background for astrophysical neutrinos
  - Beam for high-energy physics (charm, neutrino properties)
- Experimental status (5 yrs)
  - Beginnings of KM3NeT
  - IceCube Gen2 (PINGU + HEX) proposal & start?
- Opportunities
  - Determine the level of charm and prompt  $\nu$
  - Mine accelerator data for hadronic interactions (recall Sanford & Wang, BNL, AGS internal report, 1967)
  - Determine flavor ratio of astrophysical  $\nu$  at Earth
- Longer term
  - Operations of next generation detectors

# From HESE 3 yr paper appendix\*

	all energies							
	Muons	$\pi/K$ atm. $\nu$	Prompt atm. $\nu$	$E^{-2}$ (best-fit)	$E^{-2.3}$ (best-fit)	Sum ( $E^{-2}$ )	Sum ( $E^{-2.3}$ )	Data
Tot. Events	$8.4 \pm 4.2$	$6.6^{+2.2}_{-1.6}$	< 9.0 (90% CL)	23.8	23.7	38.8	38.7	37 (36)
Up	0	4.2	< 6.1	8.3	9.4	12.4	13.5	9
Down	8.4	2.4	< 2.9	15.5	14.4	26.3	25.2	27
Track	$\sim 7.6$	4.5	< 1.7	4.6	4.3	16.7	16.4	8
Shower	$\sim 0.8$	2.1	< 7.2	19.2	19.5	22.1	22.4	28
Fraction Up	0%	63%	68%	35%	40%	32%	35%	25%
Fraction Down	100%	37%	32%	65%	60%	68%	65%	75%
Fraction Tracks	> 90%	69%	19%	19%	18%	43%	42%	24%
Fraction Showers	< 10%	31%	81%	81%	82%	57%	58%	76%

	60 TeV < $E_{\text{dep}}$ < 3 PeV							
	Muons	$\pi/K$ atm. $\nu$	Prompt atm. $\nu$	$E^{-2}$ (best-fit)	$E^{-2.3}$ (best-fit)	Sum ( $E^{-2}$ )	Sum ( $E^{-2.3}$ )	Data
Tot. Events	0.4	2.4	< 5.3	18.2	18.6	21.0	21.4	20
Up	0	1.5	< 3.7	6.7	7.2	8.2	8.7	5
Down	0.4	0.8	< 1.6	11.6	11.4	12.8	12.7	15
Track	$\sim 0.4$	1.7	< 1.0	3.8	3.5	5.8	5.5	4
Shower	$\sim 0.0$	0.7	< 4.2	14.4	15.1	15.2	15.8	16
Fraction Up	0%	64%	70%	37%	39%	39%	41%	25%
Fraction Down	100%	36%	30%	63%	61%	61%	59%	75%
Fraction Tracks	> 90%	71%	20%	21%	19%	28%	26%	20%
Fraction Showers	< 10%	29%	80%	79%	81%	72%	74%	80%

\*IceCube Collaboration, arXiv:1405.5303v2